



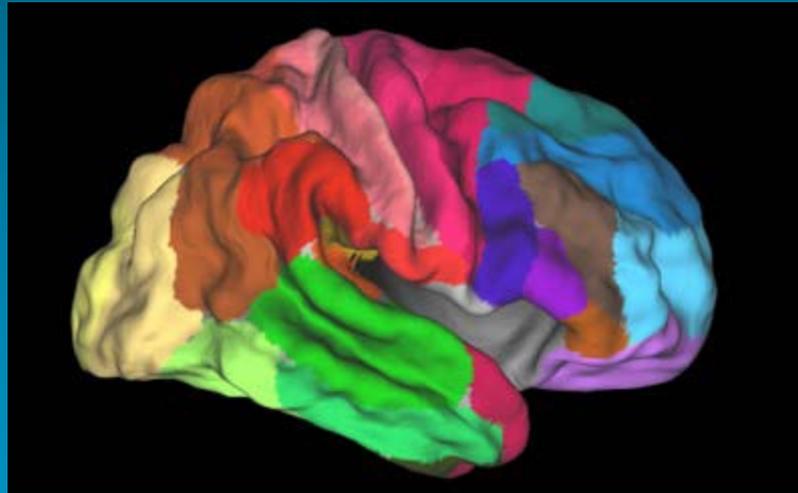
SISSA

# SPACEBRAIN

where in our inner space,  
among its **multiple** areas,  
do we construct our internal  
representations of outer space?



limbo

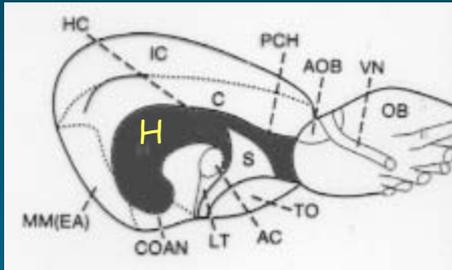


TABIS 2013, Beograd

September 20, 2013

Alessandro Treves

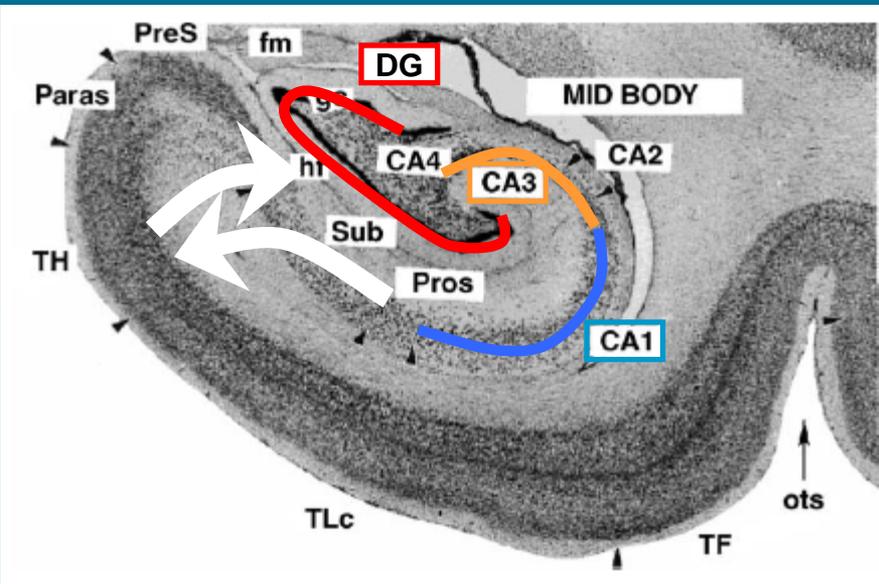
# THE HIPPOCAMPUS



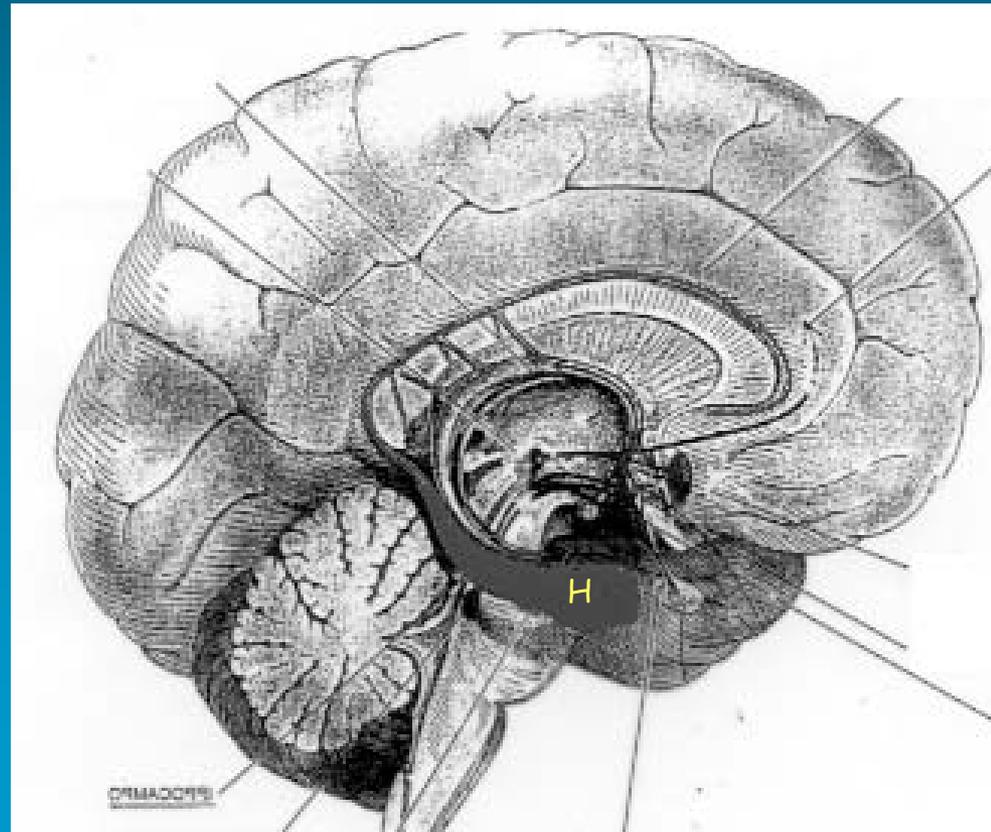
opossum

a structure which remains stable and self-similar across mammalian species

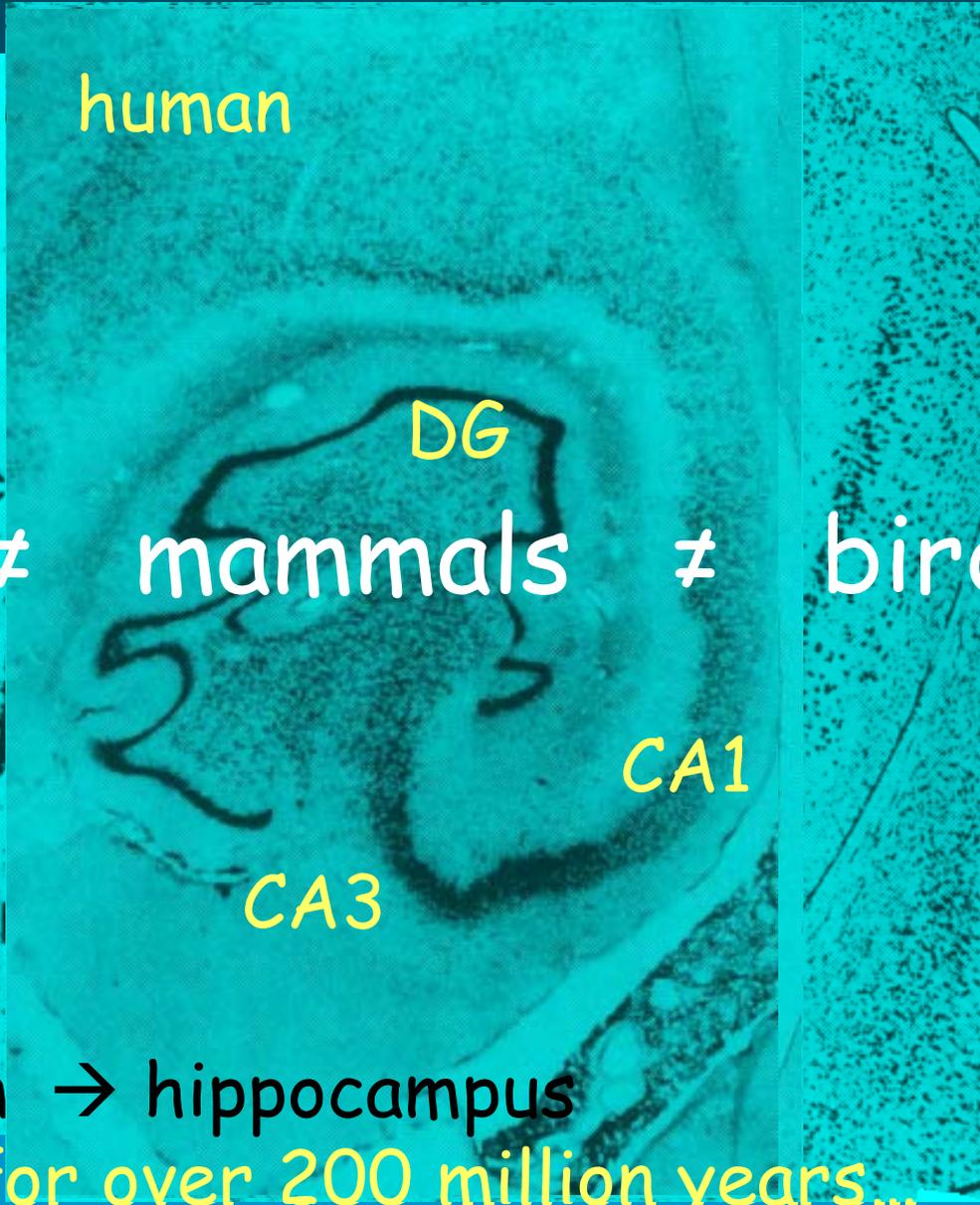
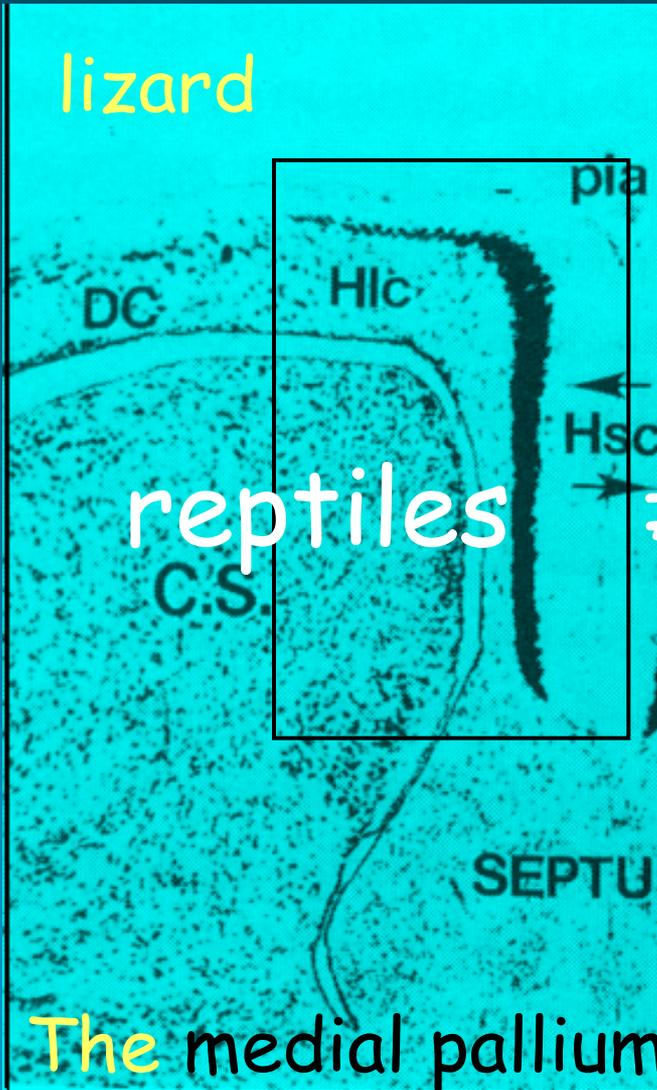
human



monkey



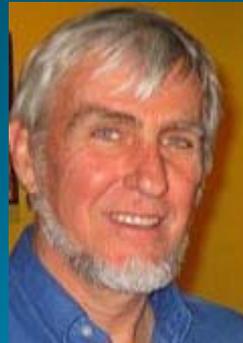
but... has it always been like that?



reptiles ≠ mammals ≠ birds

The medial pallium → hippocampus  
has been with us for over 200 million years...

# Is the hippocampus what we use to navigate?



John O'Keefe  
1971  
Univ Coll London  
SPACEBRAIN



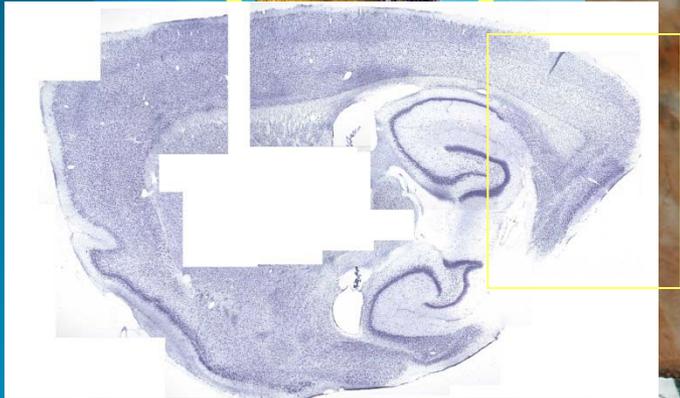
...or is it used to recollect from the past salient episodes of our lives?

# Laura and a rat



Place cells

# Neurophysiology + Neuroanatomy



Marianne Fyhn  
in the Mosers' lab  
with Menno Witter  
(Science, 2004)



ser  
ry



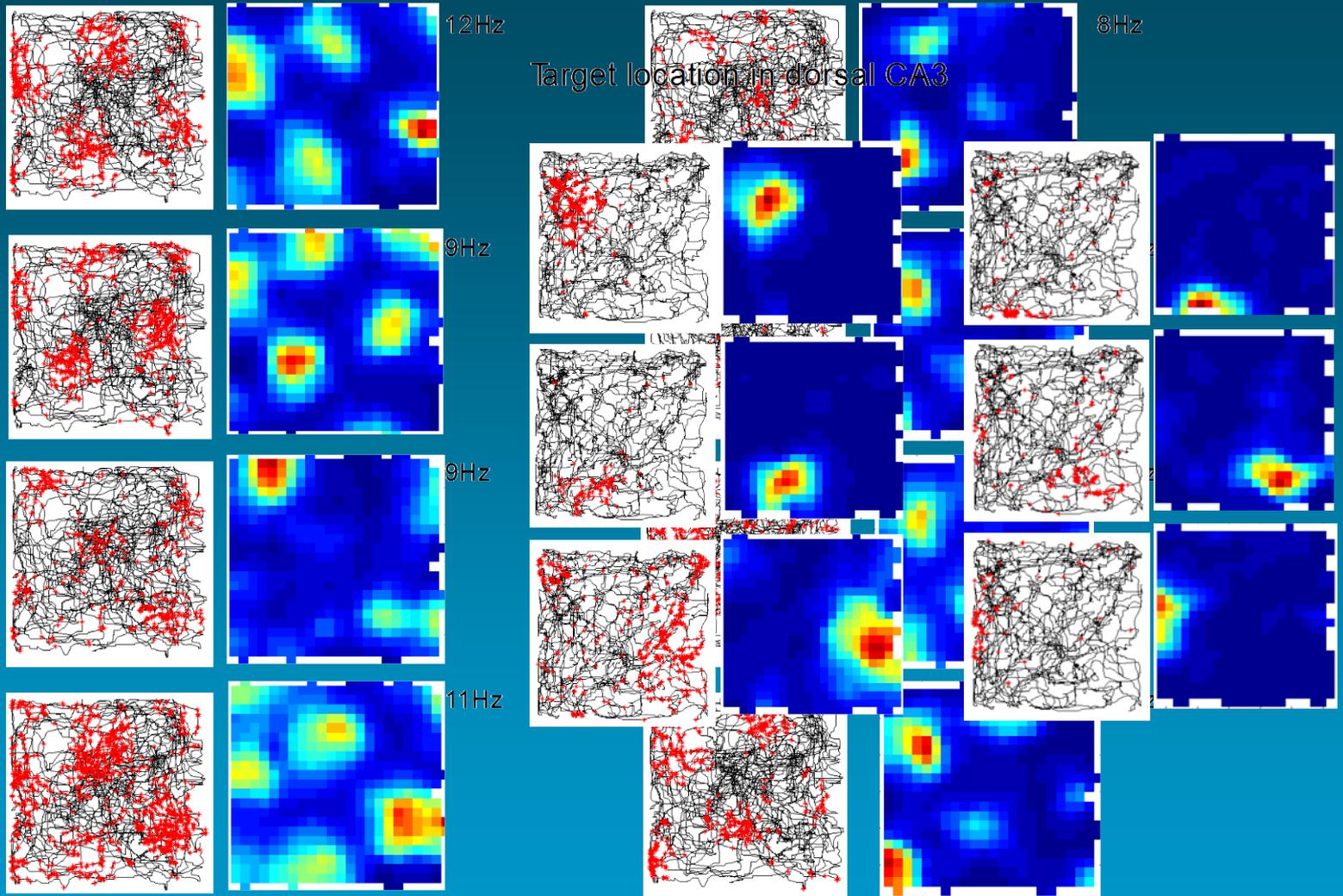
Electrodes  
were placed in  
layers II and  
III of caudal  
medial  
entorhinal  
cortex (which  
projects to  
dentate/CA3  
and to CA1,  
respectively)



AIN

# Multiple place fields in entorhinal cortex become single fields in CA3

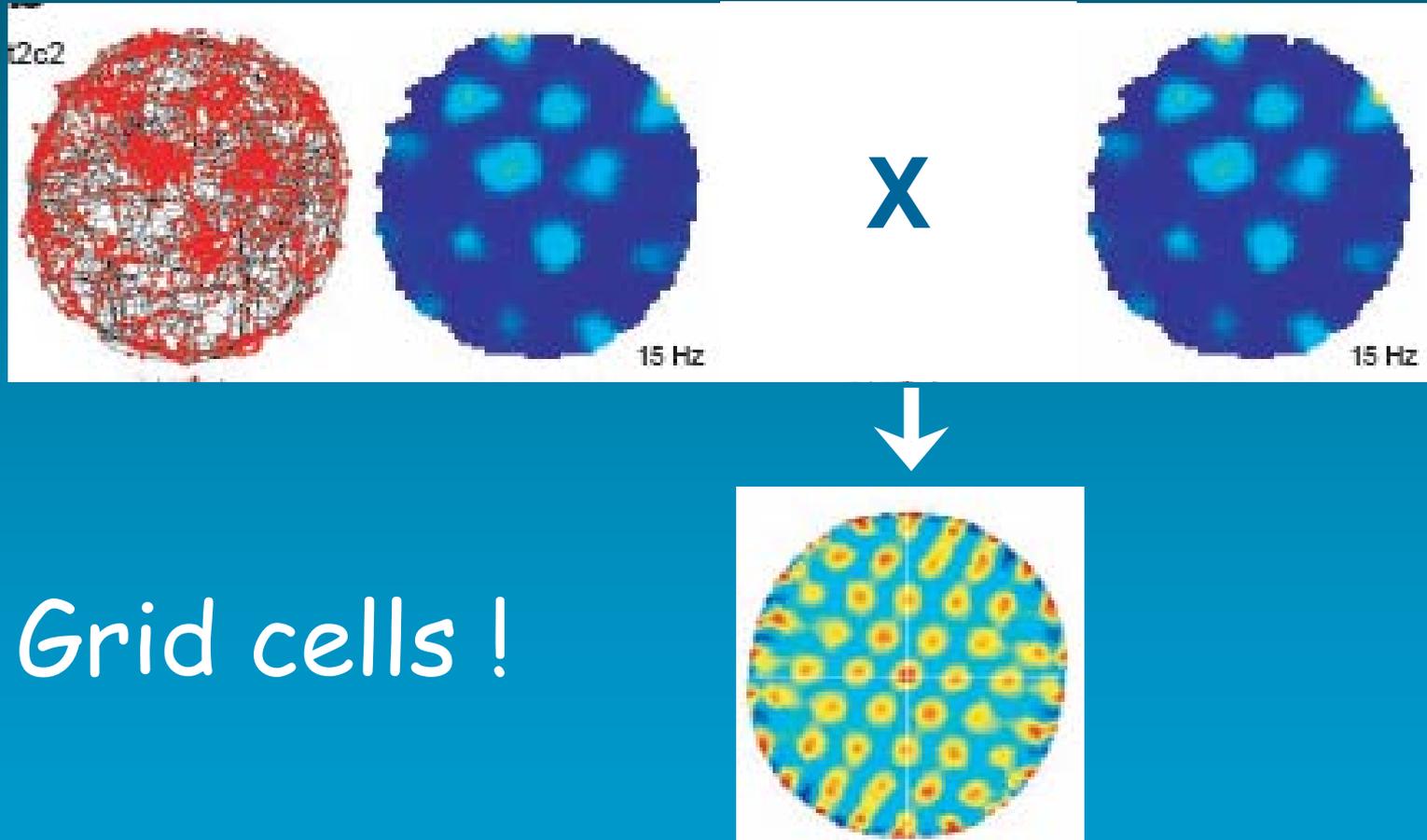
10073\_170103\_04:



Cells in dorsal medial entorhinal cortex have multiple dispersed fields

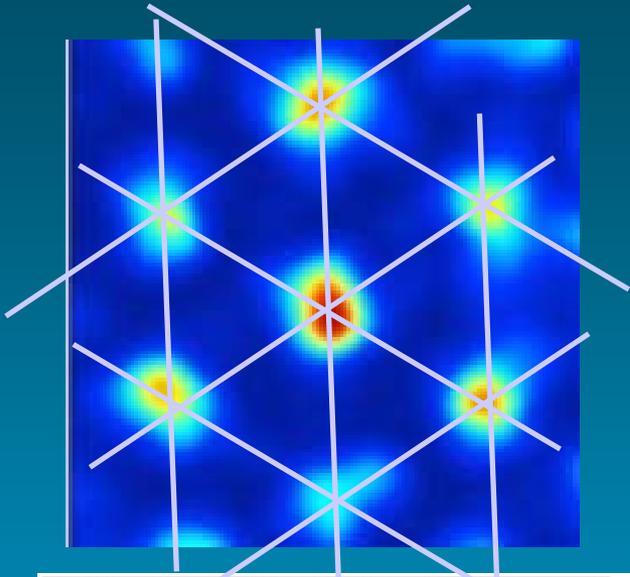
Torkell Hafting  
(with Marianne Fyhn  
et al in the Mosers' lab  
Nature, 2005)

recorded units in a  
larger environment  
and looked at the map  
autocorrelation

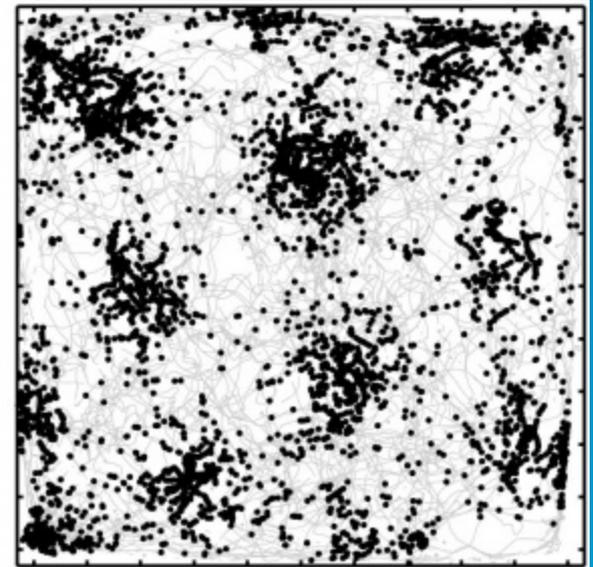
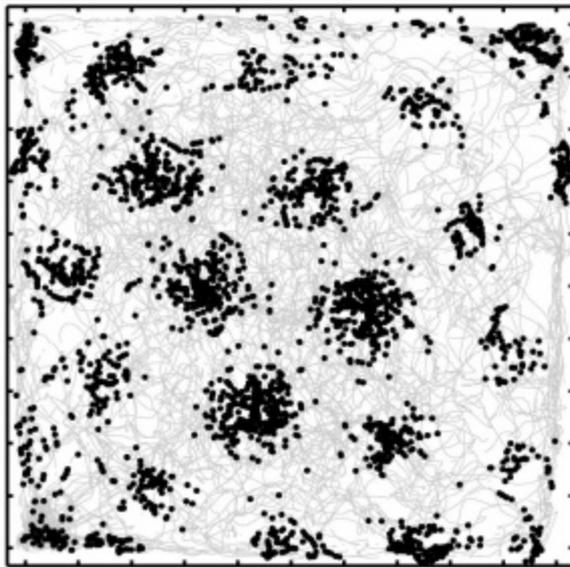
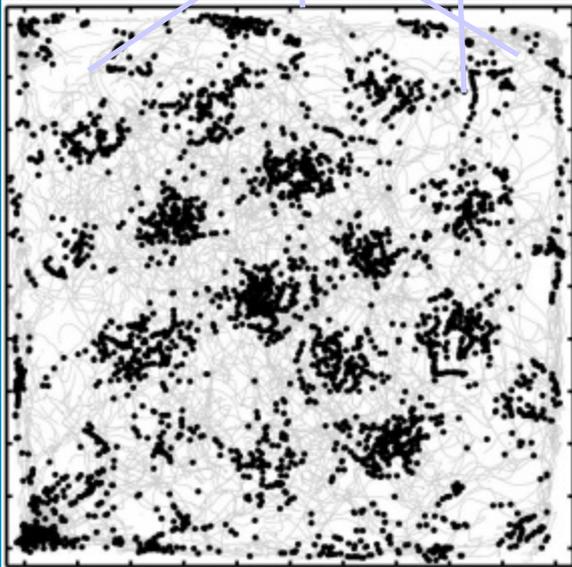


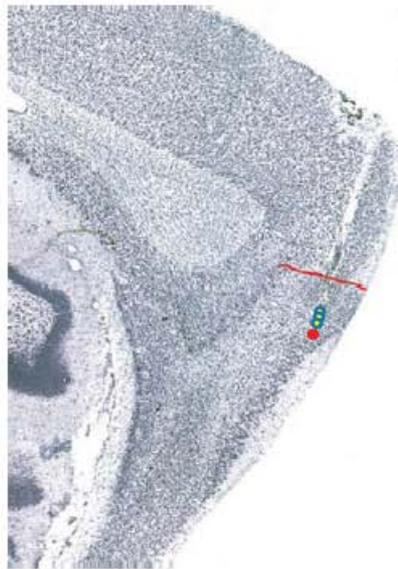
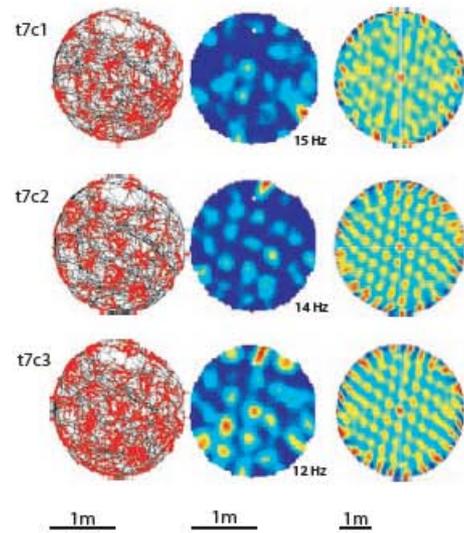
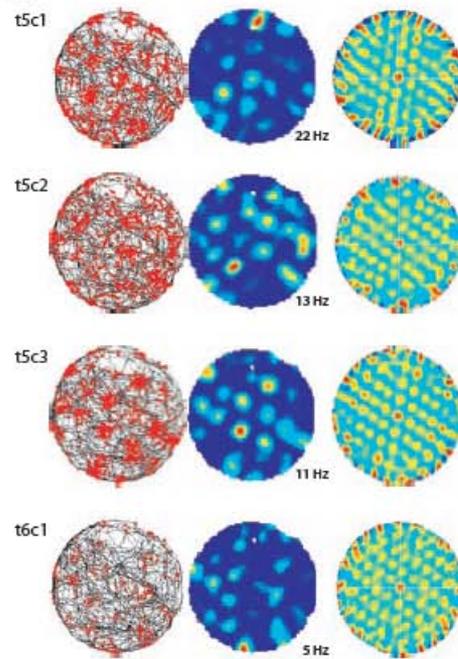
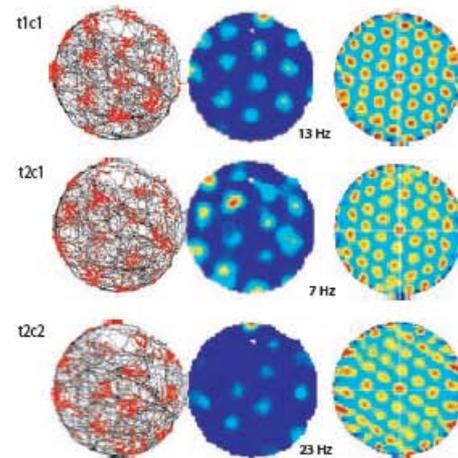
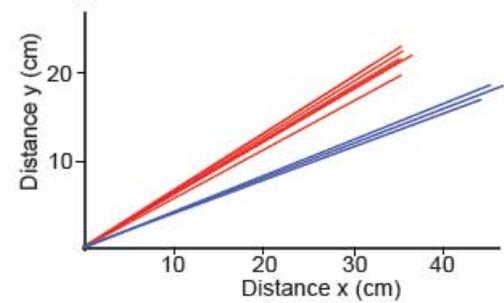
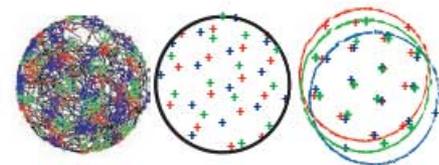
Grid cells !

Just look at one grid cell...

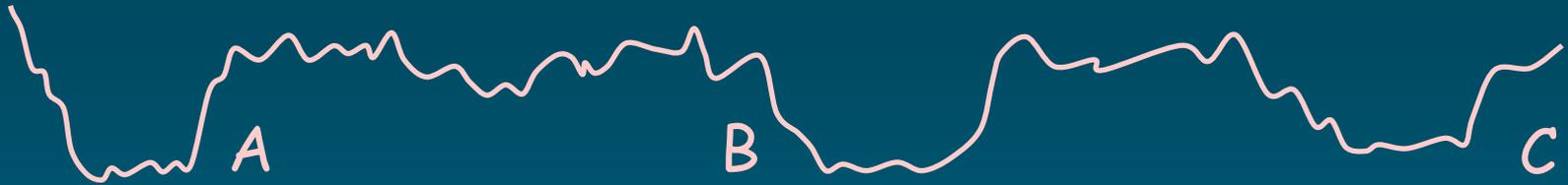


Is it just more beautiful than a place cell, more metrical, more...

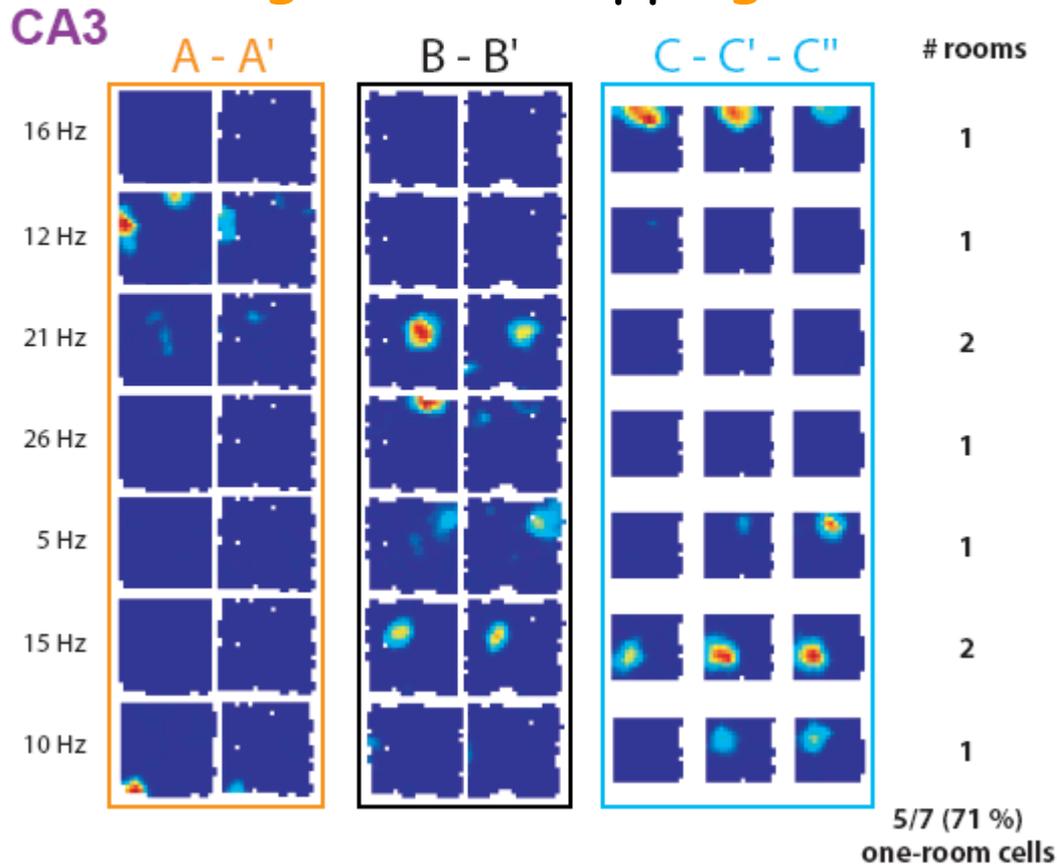


**a****b****c****d****e****f**

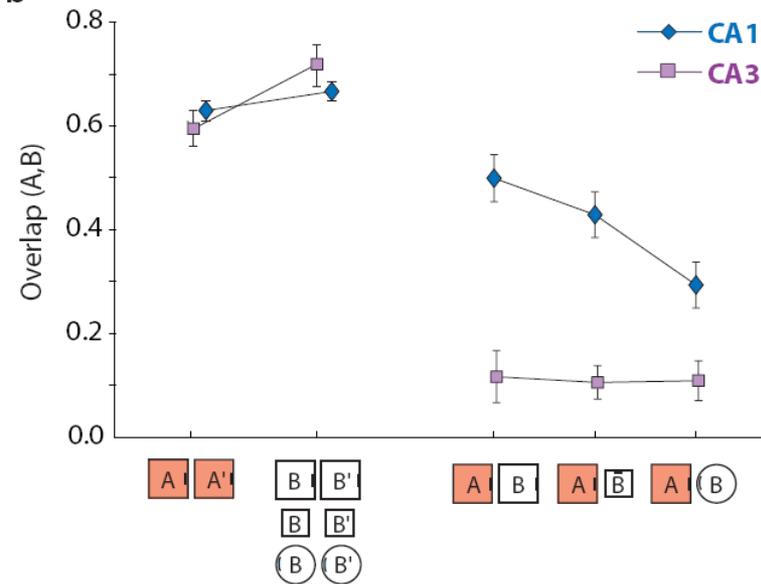
# Consider what happens in the hippocampus when changing context



'global remapping'

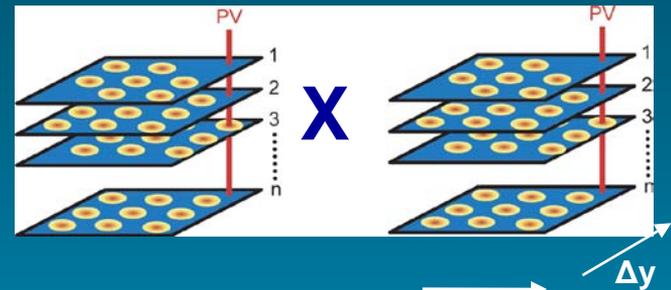


CA3 charts can be described as a (discrete?) number of continuous attractors, with minimal overlap among them

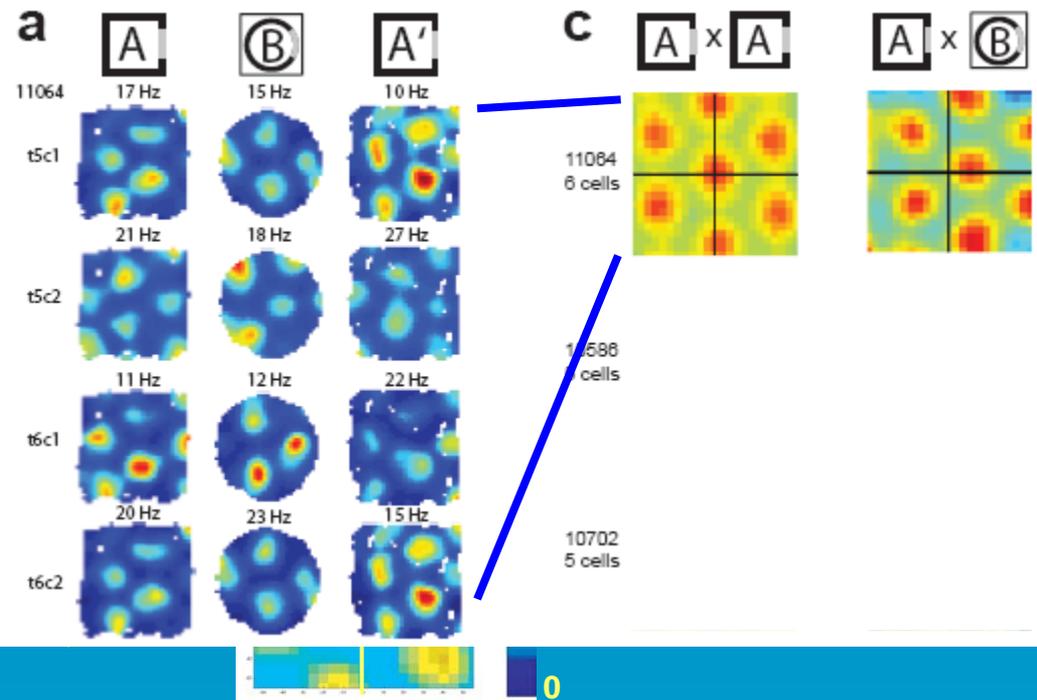


# Neurophysiology + Neural Computation

Matrices of population vectors were cross-correlated between two boxes

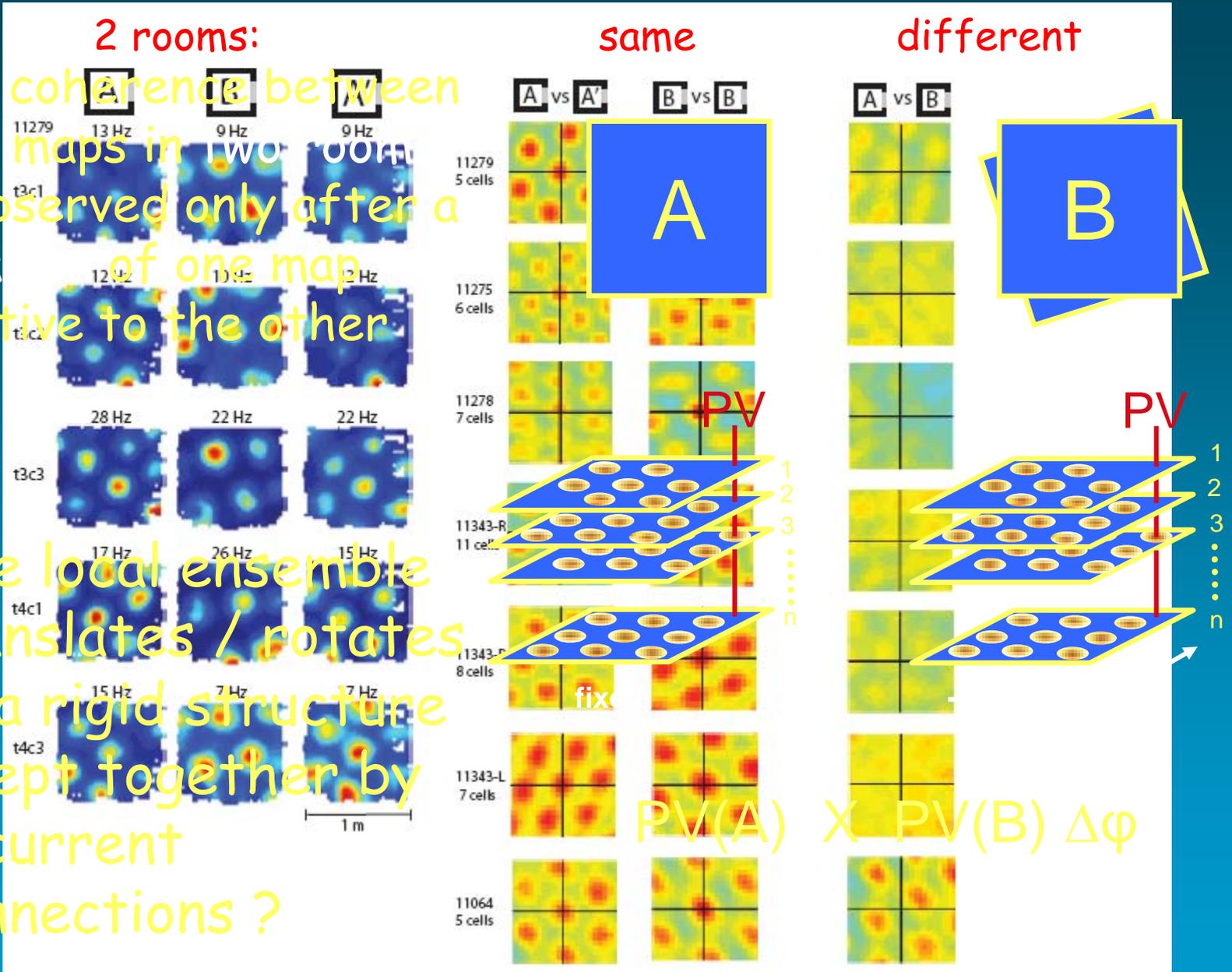


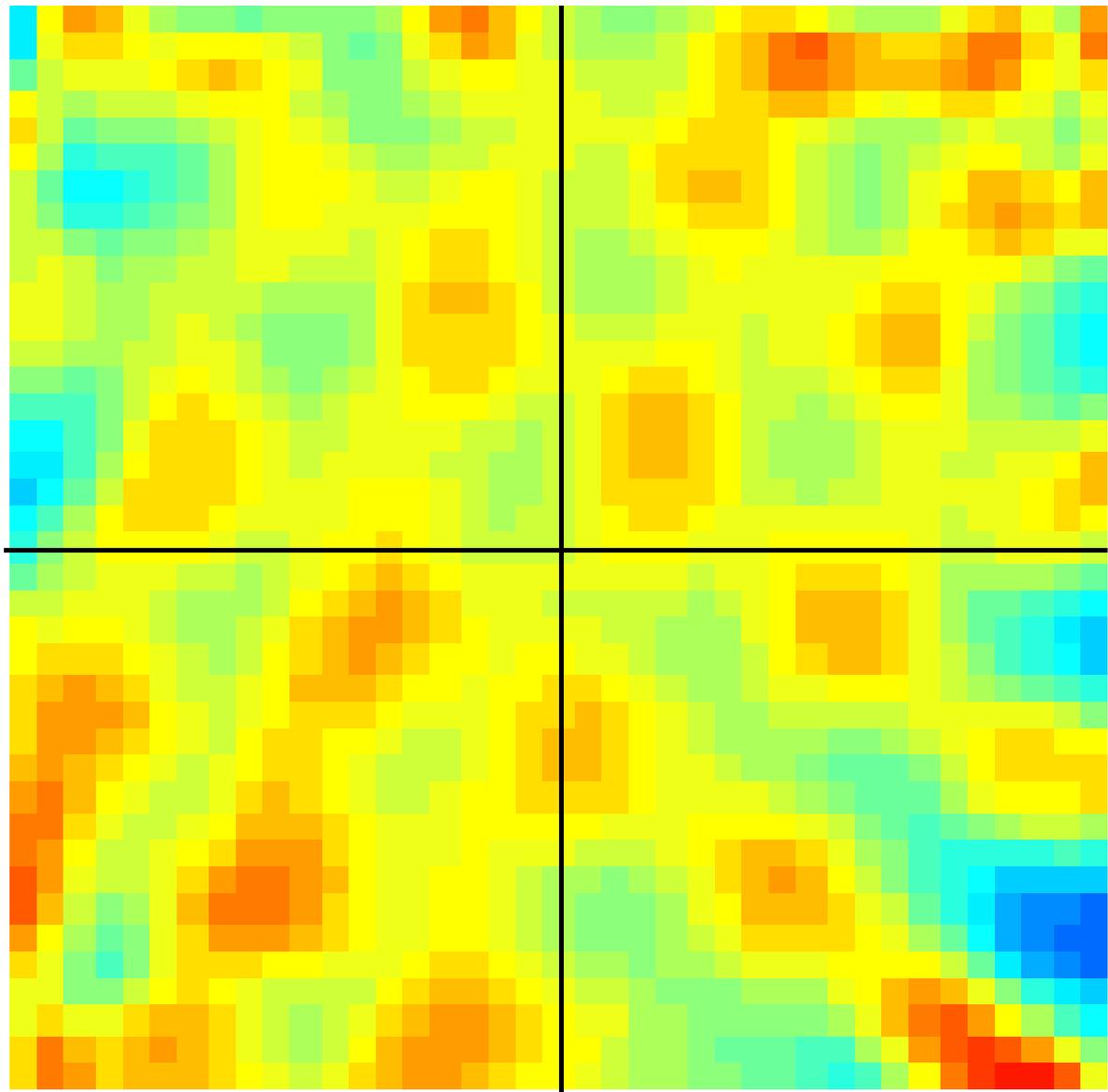
coherent displacement of the entorhinal map during global remapping in the hippocampus!



The coherence between grid maps in two rooms is observed only after a rotation of one map relative to the other

The local ensemble translates / rotates as a rigid structure ...kept together by recurrent connections ?





Thus, the intrinsic structure of the map (spacing, orientation, spatial phase) is retained,

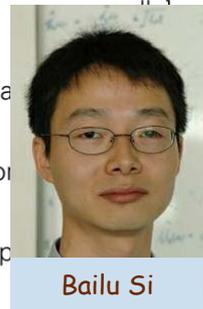
i.e. a single map may be applied rigidly in all environments

..millimeter paper

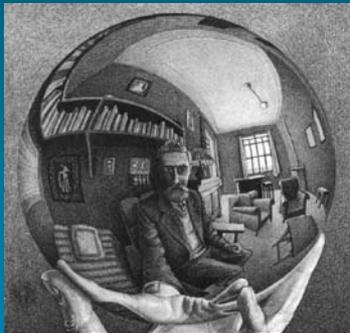
Many models have been proposed..



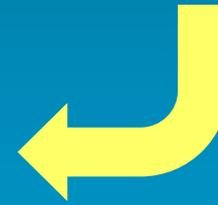
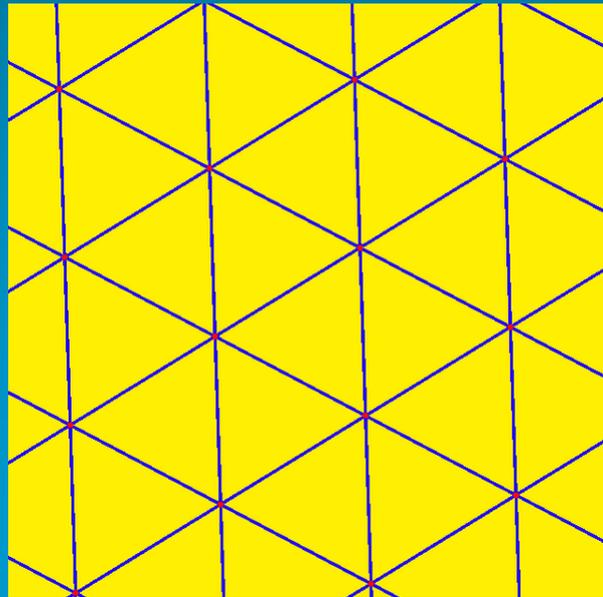
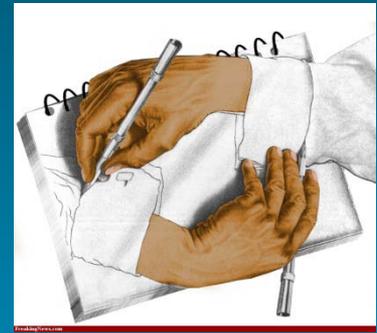
Grid cell model	Position representation	Updating mechanism
Conklin and Eliasmith (2005)	Torus attractor, single bump	Direction-conjunctive cells
O'Keefe and Burgess (2005)	[Torus attractor, single bump]	[Direction-modulated recurrent connections]
Fuhs and Touretzky (2006)	Aperiodic attractor, multi-bump	Direction-conjunctive cells
McNaughton et al. (2006)	[Torus attractor, single bump]	[Direction-conjunctive cells]
Blair et al. (2007)	[Theta grids]	-
Burgess et al. (2007)	Sinusoid phase difference	Frequency modulation
Gaussier et al. (2007)	Firing rates as coordinates	Firing rate modulation
Giocomo et al. (2007)	Sinusoid phase difference	Frequency modulation
Guanella et al. (2007)	Twisted-torus attractor, single bump	Dynamic recurrent connections
Blair et al. (2008)	[Biased ring attractor phase difference]	[Direction-conjunctive cells]
Burgess (2008)	Sinusoid phase difference	Frequency modulation
Hasselmo (2008)	Sinusoid phase difference	Frequency modulation
Hasselmo and Brandon (2008)	Firing rate	Frequency modulation
<b>Most models require an engineer inside the brain to set them up</b>		
Burak and Fiete (2009)	Torus and aperiodic attractors, multi-bump	Direction-conjunctive cells
Mhatre et al. (2012)	[Unbiased ring attractor]	[Direction-conjunctive cells]
Zilli and Hasselmo (2010)	on pha	frequency
Navratilova et al. (2012)	tractor	ion n-conjunctive cells
Welday et al. (2011)	actor p	on-conjunctive

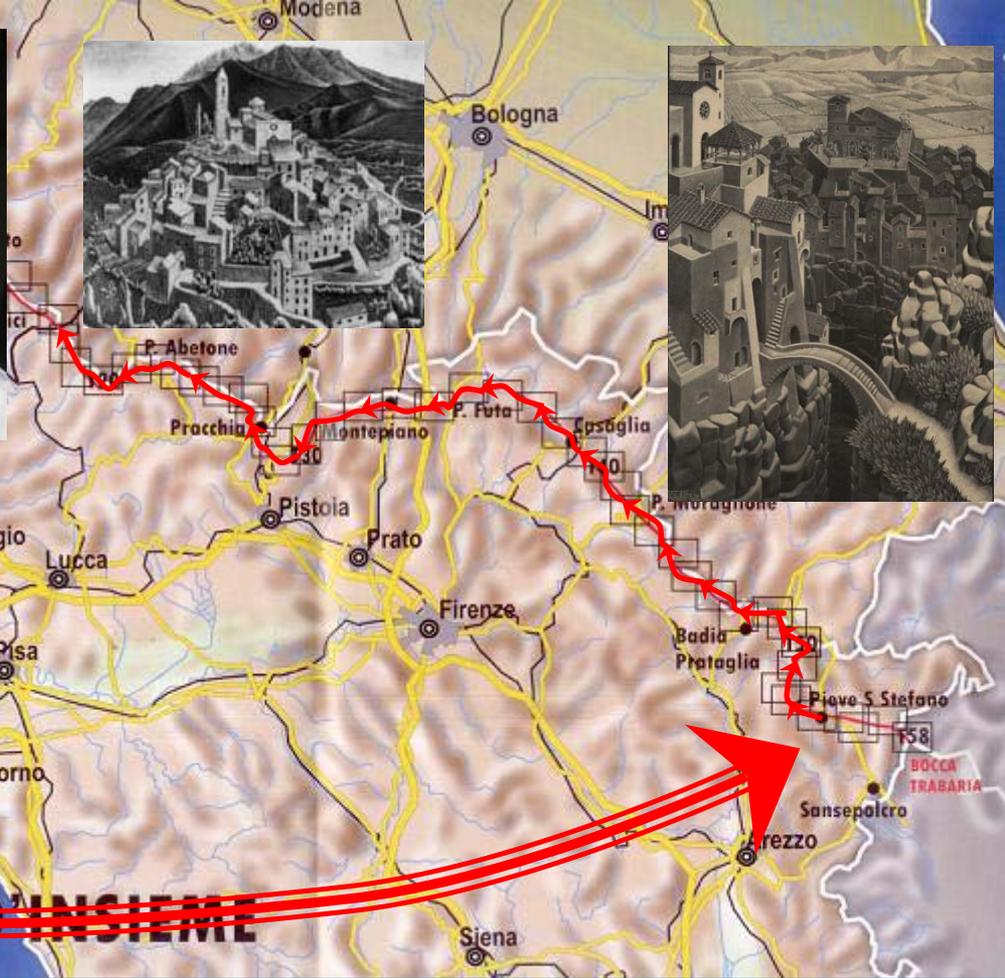
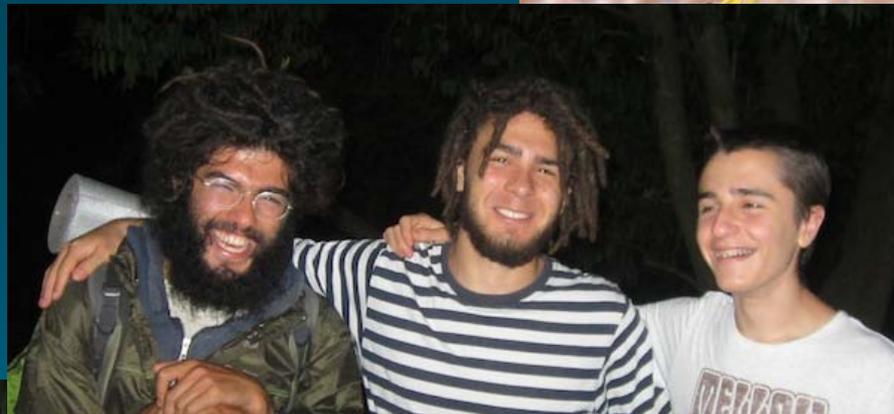


# How to decide which model is right?



In a plain box,  
with nothing inside  
all models work fine

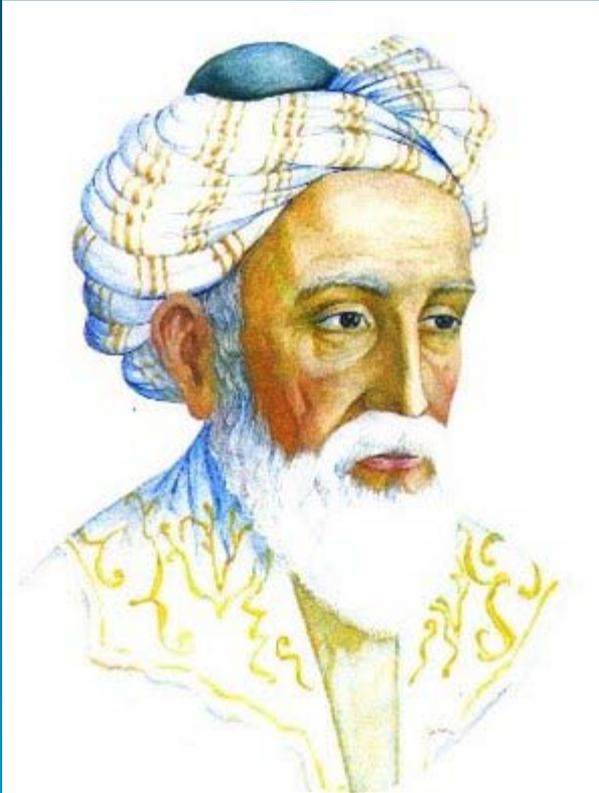




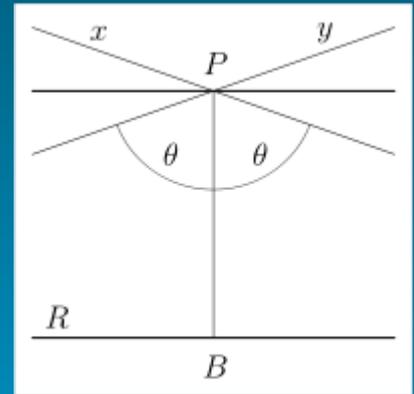
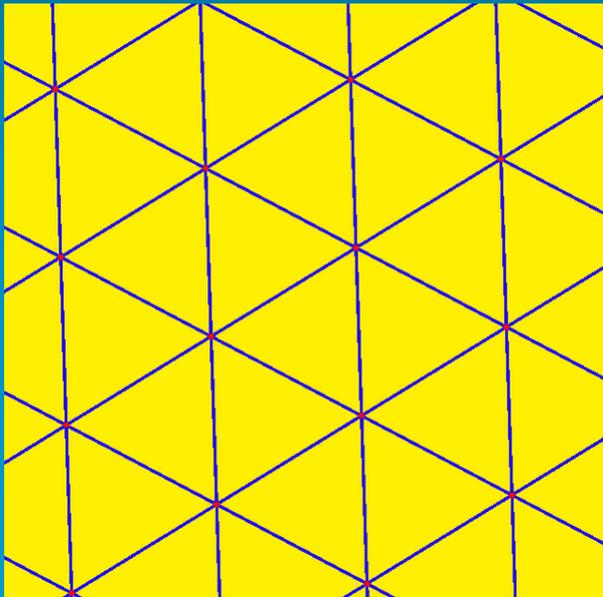
# Grande Escursione Appenninica

..no straight lines

Is it true that  
through a given  
point there can only  
be one parallel line?



Omar Khayyam  
ca. 1080

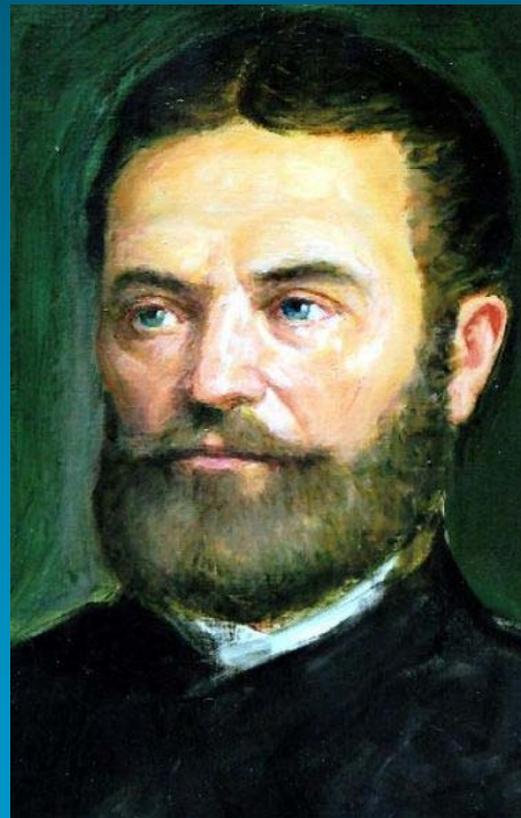
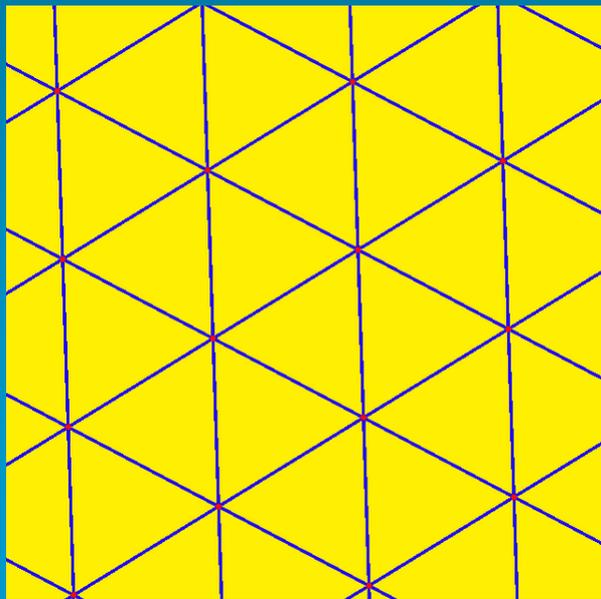


mmmhh...  
...thinking about it...  
...no!  
There can be more

ca. 1830

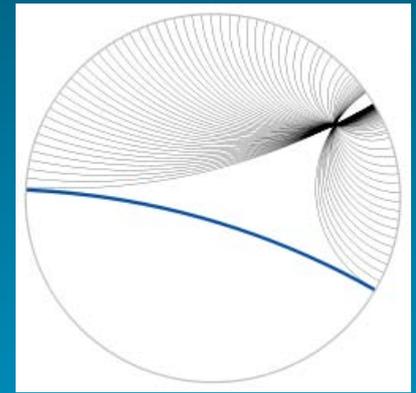
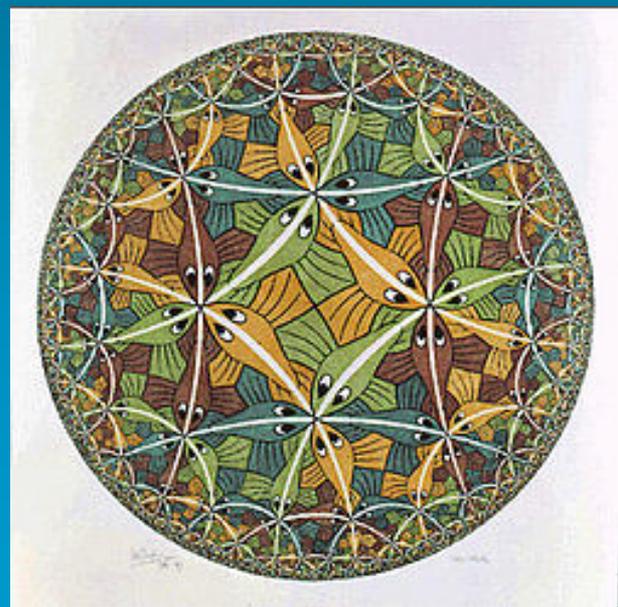


Lobachevsky



Bolyai

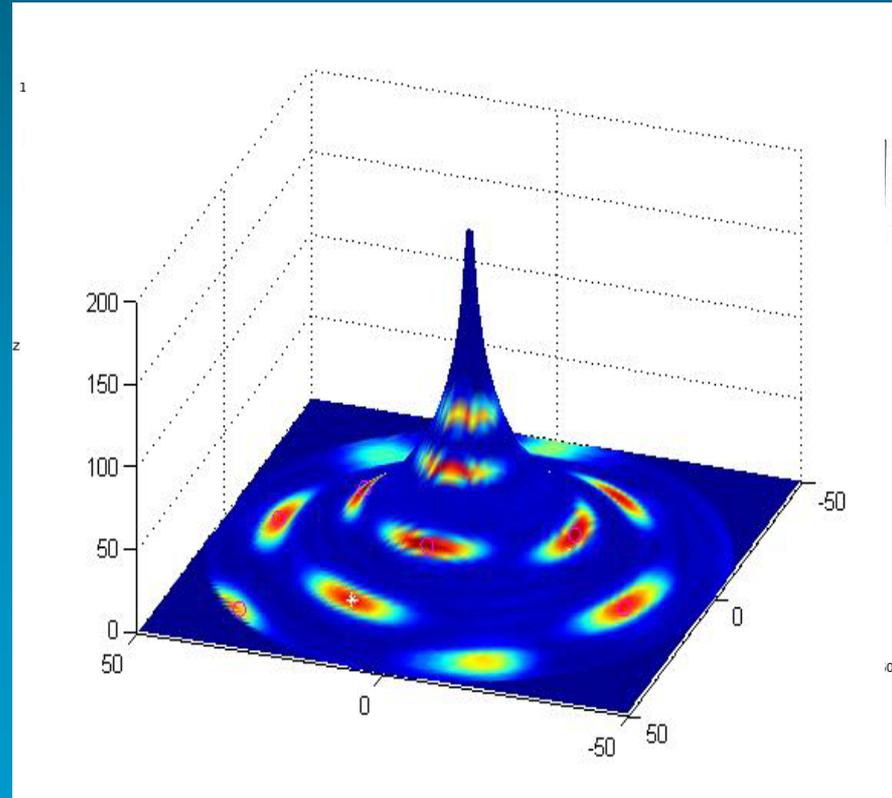
In fact !  
It all depends what  
you mean with  
*a line*  
Think of projecting it..



Hyperbolic disk



Hyperbolic  
"pseudosphere"



..a simpler experimental test of the adaptation model is to raise rodents either **in** or **on** a ball

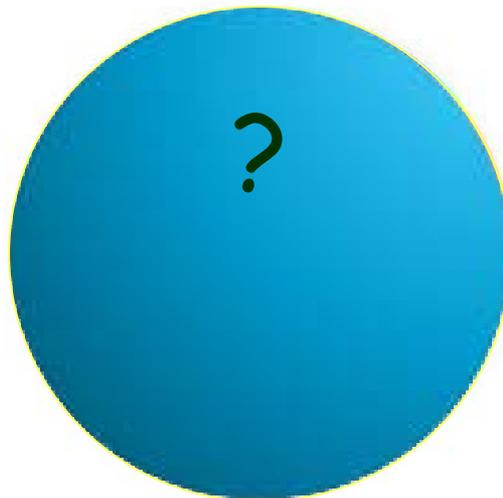
## Spherical harmonics

$$\Psi_{l^*}(r) = \sum_{l=0, l^*} \sum_{m=0, m^*} a_{lm} Y_l^m(r)$$

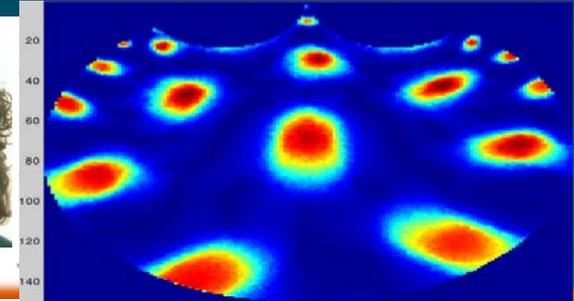


$$\begin{aligned} \Psi_6(\theta, \varphi) &= d[cY_0^0 + [aY_6^0 + \frac{b}{2}(Y_6^{-5} - Y_6^5)]] \\ &= d[\frac{c}{2}\sqrt{\frac{1}{\pi}} + \\ &\quad + [\sqrt{\frac{143}{137\pi}} \frac{1}{32} * (231 \cos^6(\theta) - 315 \cos^4(\theta) + 105 \cos^2(\theta) - 5) + \\ &\quad + \frac{143}{137\pi} \frac{21}{6} * \cos(5\varphi) \sin^5(\theta) \cos(\theta)]] \end{aligned} \quad (9)$$

what do we expect to see on the ball?

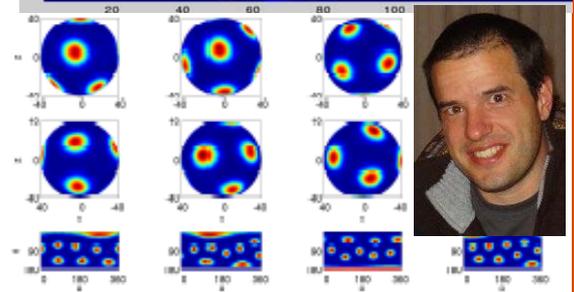


Feder  
on the

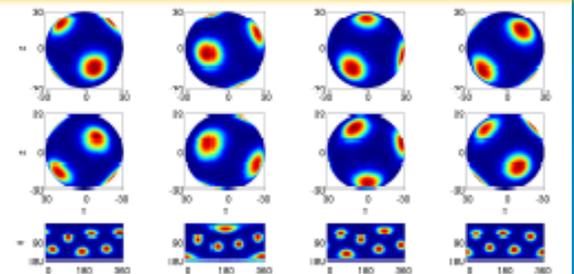


$R = 40cm$

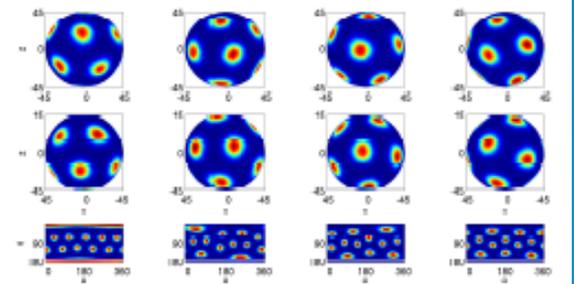
Also for mixed states



(d)  
 $R = 30cm$



(e)  
 $R = 45cm$



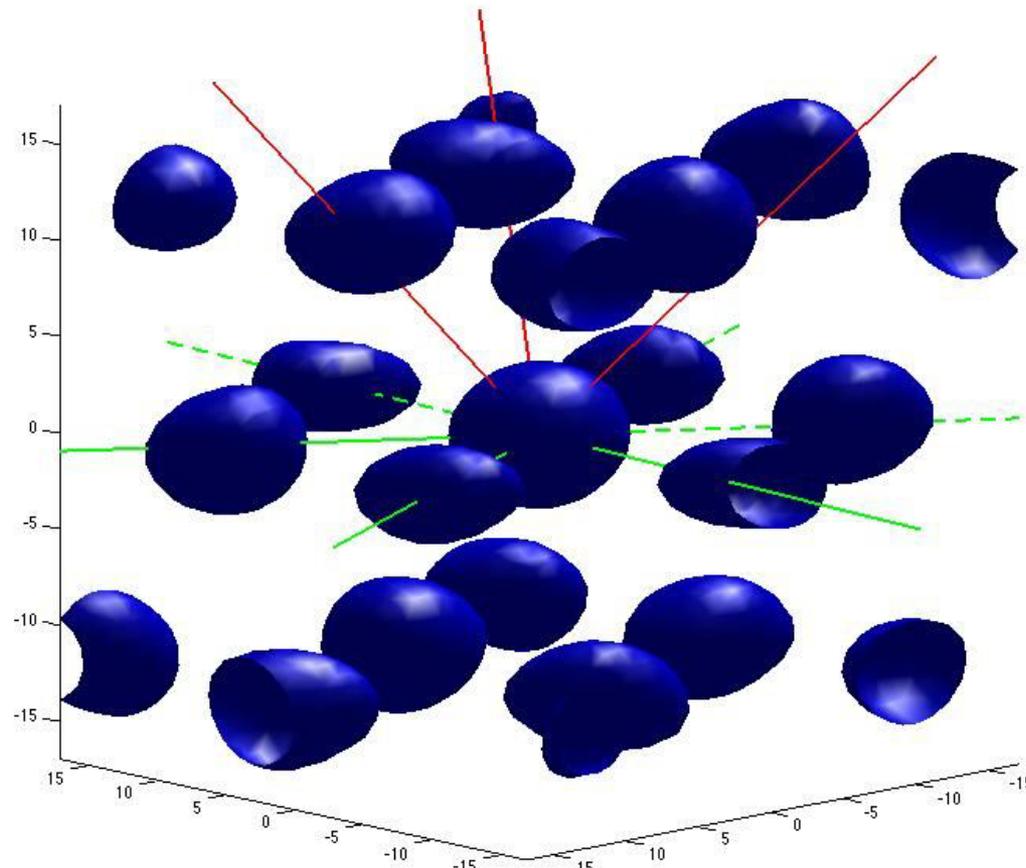
Simulations confirm the analysis

# What to expect in 3D?

(soon to be discovered by Nachum Ulanovsky)



FCC  
lattice



(or HCP  
or mixed)

Rather than Euclides or Kant, the space of one's experience

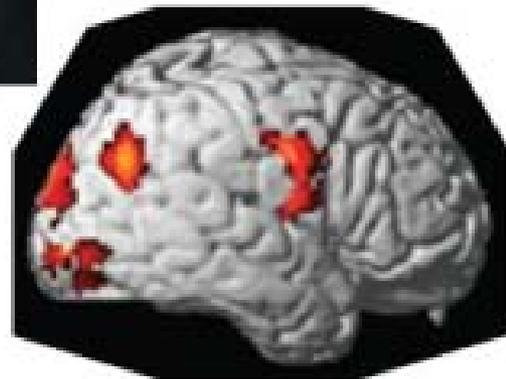
expression

# Free-energy landscape

identification

prediction

?



identity